



Research Article

Volume 14 Issue 1 - February 2018  
DOI: 10.19080/ARTOAJ.2018.14.555907

Agri Res & Tech: Open Access J  
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# The Relationship between Yield Parameters and Morphological Characters for Barley: Evaluating linear and Non-linear models



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**Submission:** January 15, 2018; **Published:** February 15, 2018

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## Abstract

The best statistical model (linear or non-linear) for use in the study of the relationship between yield parameters and morphological characters of barley was investigated. It was confirmed that Non-linear model (Exponential regression analysis) is better than linear for studying the relationship between yield parameters and morphological characters, because the determination coefficient for non-linear model was higher than the determination coefficient for linear model. Moreover, the residual distributions for non-linear equation were much better than the residual distributions for linear equation.

A relationship between leafiness and yield parameters was not shown by both linear and non-linear models, while analysis of variance (ANOVA) indicated a positive significant difference in yield according to levels of leafiness. Consequently, yield parameters had been affected by morphological characters. The non-linear model for the study of the relationship is suitable for forecasting yield.

**Keywords:** Barley breeding; Exponential; Linear; Multiple regression analysis

## Introduction

Barley is the fourth world's cereal production after wheat, rice and maize. It is the second most important cereal crops in Syria after wheat. It is one of the most suitable cereal crops, which can survive and grow over a wide range of soils and under many adverse climatic conditions compared with many other cereal crops [1].

Multiple regression analysis is frequently used to study the effect of sets of independent variables, X, on one variable Y [2]. Multiple linear regression has been employed in agricultural research. For example, in 1990, Lungu [3] applied multiple linear regression to wheat in order to study the intra- and intergenerational relationship among yield components and characteristics. He suggested that 1000-kernel weight, grain yield per plant and number of tillers per plant (in that order) were the most significant variables affecting yield.

Many agronomic barley experiments employed multiple linear regression analysis, and most of them used this kind of analysis to increase barley yield. For example, multiple linear regression has been used to identify climatic factors effecting

barley yield [1]. The latter studied the effects of weather on grain yield over a 15-year period. Multiple linear regression analysis was also used to predict cadmium concentrations and PH in barley grain by testing soil properties [2].

Multiple regression has been compared with an artificial neural network model. For example, in 2011, Zaefizadeh compared multiple linear regressions (MLR) and artificial neural networks (ANN) in predicting barley yield. They found that the neural network for estimating barley genotypes yield was more effective than a regression approach, because the degree of error in multiple linear regression model was greater than in the artificial neural network [3]. Also, multivariate regression and artificial neural network have been used to predict barley production from soil characteristics in northern Iran [4]. The latter indicated that artificial neural network is a more powerful tool than multivariate regression for the prediction of the biomass and grain yield of barley from soil properties. In 2013, Paswan and Begum used regression and neural network models for the prediction of crop production. Paswan and Begum found that neural network models were more powerful than linear

regression for data analysis. However, they found there was an overlap between the two fields and there were several models that could be used by neural networks [5].

Multiple linear regression analysis was applied to barley data in Egypt to identify and qualify the relationship between grain yield and morphological characters [6]. He found that the grain yield strongly and positively correlated with grain numbers per spike, grain weight/spike, 1000-grain weight, number of spikes per square meter and spike length.

In 2015, Dorostkar et al. [7] studied the relationship between grain yield and yield components, using multivariate analysis in barley cultivars. They used correlation coefficient, regression and path analysis for the analysis of data. It was found that path analysis was the best model for showing the relationship between grain yield and yield components. These models of analysis showed that the spikes per square metre had a negative correlation with kernels per spike, kernel weight and the effects of spikes per square metre. Kernel weight of grain yield was significantly different.

Multiple linear regression analysis indicated that the parameters of high water, nutrients and ecotype plant size significantly affected plant fitness, whether estimated by reproductive biomass or by yield [8].

Multiple linear regression analysis was compared to variate models of multivariate analysis to characterize spring barley accessions. According to multiple regression analysis, 72.8% of the variance in germplasm was to be explained by plant height, lodging and grain yield [9].

Multiple non-linear regression analysis has also been used by scientists to decide whether there are relationships between variables. Some of them found linear regression analysis not to be useful and sought alternative equations. For example, non-linear regression analysis has been used to study the relationship between leaf appearance rate (LAR) and temperature in wheat trials [10]. They found that a non-linear model is better than a linear model for ascertaining the extent to which the leaf appearance has been affected by the lower root.

The ultimate goal of this research is located in two points:

- a. To choose the optimal model for studying the relationship between yield parameters and morphological characters.
- b. To indicate the most important morphological characters variables affected yield parameters.

## Materials and Methods

### Materials

Two field experiments were carried out at the experimental stations (Tel Hadya and Breda, Syria). There were 306 observations in each area (three hybrids each hybrid 102 observations). The experiments were designed as a randomized

block design, with two replicates in Tel Hadya and Breda. Seed rate was 100 (kg ha<sup>-1</sup>). Plants were fertilized according to the commercial practice.

Data are divided into two sets, morphological characters and yield parameters:

### Morphological characters

Plant height was estimated by taking the mean of three random samples from each experimental plot.

Leafiness was recorded as a five point scores estimated by eye at ear emergence.

Score 1: very low leafiness.

Score 2: low.

Score 3: medium.

Score 4: high.

Score 5: very high.

Vegetative duration was the number of days from germination until 50% ear emergence.

Length of growing season was the number of days from germination to harvest.

### Yield parameters

A. Total plant yield: a two metre plot length of barley was harvested from each experimental plot after removing the border rows. Total plant yield was recorded and expressed as kg ha<sup>-1</sup>.

B. Grain and straw yields were measured after mechanically separating grain from straw expressed as kg ha<sup>-1</sup>.

### Statistical methods

The multiple regression equation is formulated as a linear model [11,12]:

$$y = a_0 + a_1x_1 + a_2x_2 + \dots + a_nx_n$$

The multiple regression equation is formulated as an exponential model [13]:

$$y = a_0e^{a_1x_1 + a_2x_2 + \dots + a_nx_n}$$

The standard error of  $a_i$  ( $SE_{a_i}, i=1,2,\dots,p$ ) is given by the equation [14]:

Where: 
$$SE_{a_i} = \frac{S}{\sqrt{\sum (x_i - \bar{x}_i)^2}}$$

and: 
$$RSS = SSE = \sum (y_i - (\hat{a}_0 + \hat{a}_1x_1 + \dots + \hat{a}_px_p))^2$$

Each of the independent variables can be tested by the equation:

$$t = \frac{a_i}{SE_{a_i}}, \text{ where } i = 1, 2, \dots, p$$

Subsequently, an f-test was used to study the significance of these equations [21,22]

$$F = \frac{(\sum(y_i - \bar{y})^2 - \sum(y_i - \hat{y}_i)^2) / p}{\sum(y_i - \hat{y}_i)^2 / (n - p - 1)}$$

The coefficient of determination ( $R^2$ ) tells us how much of the variation in the dependent variable  $y$  is explained by the equation according to independent variables. It is given by Tabachnick & Fidell [15]:

does not indicate the significance of the regression Kollo & Rosen [16].

$$R^2 = \frac{\sum(\hat{y}_i - \bar{y})^2}{\sum(y_i - \bar{y})^2} = \frac{SS_R}{SS_y}$$

The residual are expected to be normally distributed  $\sim N(0, \sigma^2)$ . Residual plots use standardized and studentized residuals. Studentized residuals are used to find the outlier. It is given by:

$$r_i = \frac{e_i}{\sqrt{\hat{\sigma}^2(1-h_{ii})}} = \frac{e_i}{\sqrt{MS_E(1-h_{ii})}}$$

Where,  $h_{ii}$  the diagonal element of the hat matrix H.

## Results

### Total plant yield

Multiple regression analysis (linear and exponential) was used to study the relationship between total plant yield

as dependent variables ( $y$ ) and morphological characters (vegetative duration  $x_1$ , plant height  $x_2$ , length of growing season  $x_3$  and leafiness  $x_4$ ) as independent variables. The linear and exponential results are summarized in Table 1.

**Table 1:** The relationship between total plant yield and morphological characters.

Constant	26021.034***	19.202***
Vegetative duration	124.578***	0.027***
Plant height	111.159***	0.021***
Length of growing season	104.660**	0.014**
Leafiness	-141.505	0.008
R <sup>2</sup> %	64.38	71.71
R	0.802***	0.847***
P (equation sig)	<0.0001	<0.0001
P (Lack-of-Fit)	0.882	0.419

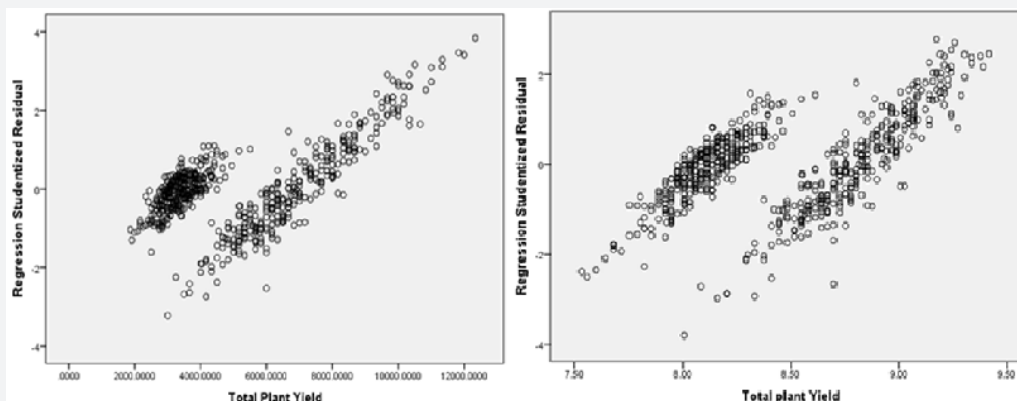
$P < 0.001$ \*\*\*,  $P < 0.01$ \*\* ,  $P < 0.05$ \*

According to Table 1, the equations were:

$$\text{Linear: } y = 26021.034 + 124.578x_1 + 111.159x_2 + 104.660x_3 - 141.505x_4$$

$$\text{Exponential: } y = 19.202e^{0.027x_1 + 0.021x_2 + 0.014x_3 + 0.008x_4}$$

There were significant multiple correlations (linear: 0.802\*\*\* and exponential: 0.847\*\*\*) between total plant yield and morphological characters. The regression coefficients for vegetative duration, plant height, length of growing season and leafiness were significant  $P < 0.05$  (linear and exponential; Table 1). 64% and 72% of the variation in the total plant yield is explained by the linear equation and exponential equation respectively. Figure 1 showed that the residual distribution for the exponential and linear equations.



**Figure 1:** The residuals between the total plant yield and morphological characters.

### Grain yield

The results for multiple regression analysis (linear and exponential) for the relationship between grain yield and morphological characters are summarized in Table 2. The regression equations are:

$$\text{Linear: } y = -13621.04 + 69.048x_1 + 45.651x_2 + 56.388x_3 - 104.064x_4$$

$$\text{Exponential: } y = 19.11e^{0.0301x_1 + 0.0179x_2 + 0.0144x_3 - 0.0038x_4}$$

Multiple regression analysis (linear, exponential) showed that grain yield was affected positively and significantly

( $P < 0.05$ ) by morphological characters except leafiness. The regression coefficient were significant ( $P < 0.05$ ) except leafiness ( $P = 0.32 > 0.05$ ; Table 2). The determination coefficients were

58.8% and 67.71% for linear and exponential equations respectively. Figure 2 showed the residuals distribution for exponential and linear equations.

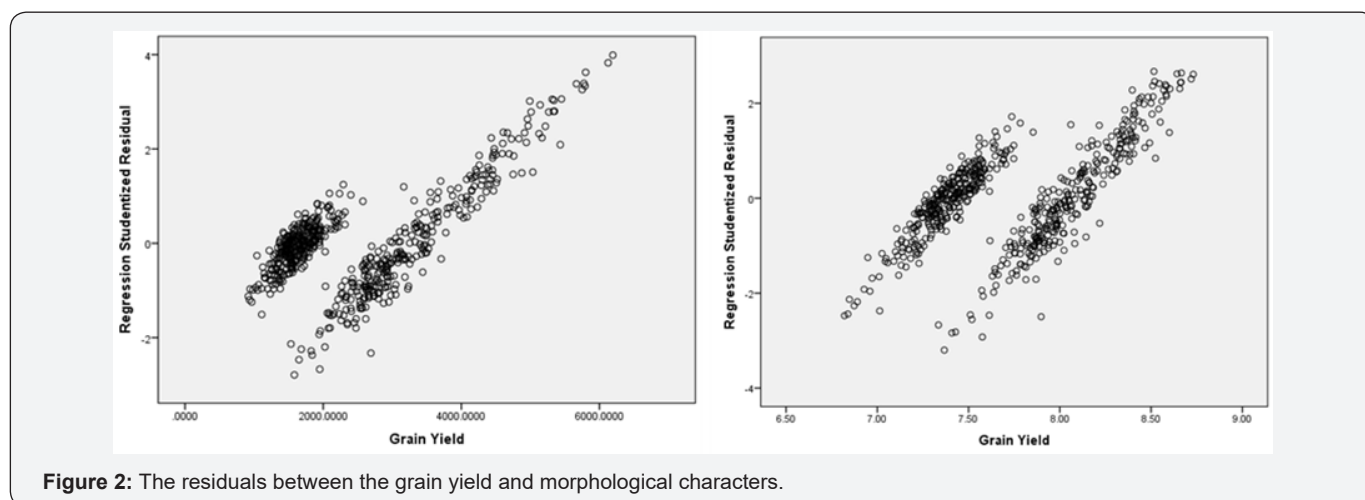


Figure 2: The residuals between the grain yield and morphological characters.

Table 2: The relationship between grain yield and morphological characters.

Step	Linear	Exponential
Constant	-13621.04***	19.11***
Vegetative duration	69.048***	0.0301***
Plant height	45.651***	0.0179***
Length of growing season	56.388**	0.0144**
Leafiness	-104.064	-0.0038
R <sup>2</sup> %	58.8	67.71
R	0.767***	0.82***
P (equation sig )	<0.0001	<0.0001

$P < 0.001$ \*\*\*,  $P < 0.01$ \*\* ,  $P < 0.05$ \*.

### Straw yield

Table 3: The relationship between straw yield and morphological characters.

Step	Linear	Exponential
Constant	-12401***	12.81***
Vegetative duration	65.5***	0.0235***
Plant height	55.5***	0.0235***
Length of growing season	48.3**	0.0125*
Leafiness	-37.5	0.021
R <sup>2</sup> %	64.5	71
R	0.803***	84.3***
P (equation sig )	<0.0001	<0.0001

$P < 0.001$ \*\*\*,  $P < 0.01$ \*\* ,  $P < 0.05$ \*.

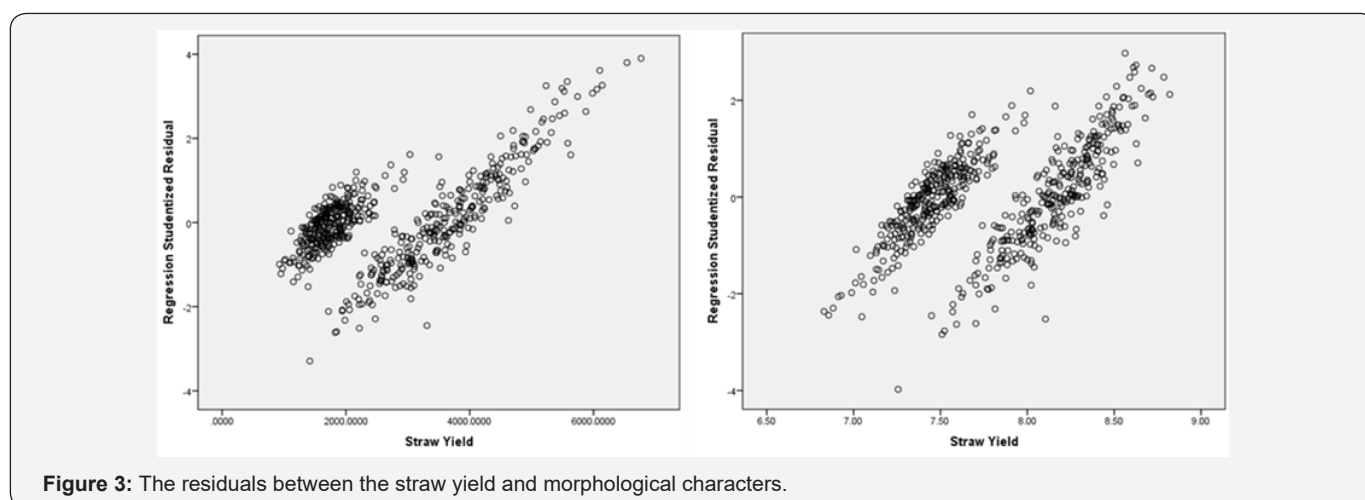


Figure 3: The residuals between the straw yield and morphological characters.

The relationship between straw yield and morphological characters was computed by using multiple regression analysis, as summarized in Table 3. The regression equations are:

$$\text{Linear: } y = -12401 + 65.501x_1 + 55.500x_2 + 48.303x_3 - 37.5x_4$$

$$\text{Exponential: } y = 12.81e^{0.0235x_1 + 0.0235x_2 + 0.0125x_3 + 0.0210x_4}$$

There were a significant relationship (linear and exponential) between straw yield and morphological characters ( $P < 0.05$ ). 64.5% and 71% of the variation in the total plant yield is explained by the linear equation and exponential equation respectively. Figure 3 showed the residuals distribution for exponential and linear equations.

## Discussion

### The relationship between total plant yield and morphological characters

The morphological character variables, except leafiness, were highly correlated (positively) with total plant yield (Table 1). These results agree with those of Žáková and Benková [9]. Thus, regression analysis showed that total plant yield was not affected by leafiness, while analysis of variance (ANOVA) indicated that total plant yield had been affected by leafiness ( $F = 11.124$ ;  $P < 0.05$ ) and the mean total plant yield at leafiness levels 4.5 and 5 were the best. When comparing models with the same number of parameters, the model with the highest significant determination coefficient ( $R^2$ ) should be selected [17]. Thus, 72% of the variation in the total plant yield is explained by the exponential equation, while 64% of variation was explained by the linear equation. Figure 1 showed that the residual distribution for the exponential equation was much better distributed than the linear equation. In the linear equation, there were forty-two points (612 points) that were more than two standardised residuals away from the expected value, but in the exponential equation, there were only thirty-two points that were more than two standardised residuals away from the expected value (according to studentized residuals  $R_i$ ).

In conclusion, the total plant yield was strongly and significantly affected by plant height, vegetative duration and length of growing season respectively. Multiple linear regression did not show how much total plant yield had been affected by leafiness. The exponential equation was better than the linear equation for studying the relationship between total plant yield and morphological characters in barley breeding trials.

### The relationship between grain yield and morphological characters

The grain yield was significantly affected by morphological characters except leafiness, while analysis of variance test (ANOVA) showed that grain yield was affected by leafiness ( $F = 9.016$ ;  $P < 0.05$ ). The least significant difference test (LSD) showed that the best grain yield was with levels of leafiness 4, 4.5 and 5. These results agree with Ohlander L, et al. [18]. Multiple regression analysis did not show this result because there were no significant differences for grain yield between levels of leafiness 2, 2.5, 3 and 3.5. Also there were no significant difference in grain yield by the levels of leafiness 4, 4.5, 5. Thus, the grain yield had two levels according to leafiness, the first one with level 2, 2.5, 3 and 3.5 and the second level of grain yield was with level of leafiness 4, 4.5 and 5. These results agree with those of Žáková & Benková [9]. Grain yield was affected by vegetative

duration slightly more than by plant height, because the simple correlation between vegetative duration and grain yield ( $R = 0.74$ ;  $P < 0.01$ ) was higher than the simple correlation between grain yield and plant height ( $R = 0.72$ ;  $P < 0.01$ ). According to Table 2, the multiple regression in the linear and exponential models with coefficients of determination ( $R^2$ ) value 58.8 and 67.71, 59 respectively were significantly acceptable for studying the relationship between grain yield and morphological characters. The coefficient of determination was close to a maximum of  $R^2\% = 68$  for exponential regression and  $R^2\% = 59$  for linear regression. The coefficient of determination for exponential regressions were higher than the coefficient of determination for linear regression. Figure 2 showed that, the residuals distribution for exponential equation was much better than the residuals distribution for linear equation. Also, according to studentized residuals  $R_i$ , Forty-two points (612 observations) were more than two standardised residuals away from the expected value for linear equations, while in the exponential equation there were thirty-eight points only (Figure 2). In conclusion, the grain yield was significantly affected by morphological characters. The determination coefficient and the distribution of the residuals indicated that the exponential equation were better than the linear equation for studying the relationship between grain yield and morphological characters.

### The relationship between straw yield and morphological characters:

Plant height had the greatest influence on straw yield. Vegetative duration was the second independent variable that affected the straw yield. Vegetative duration and length of growing season increased the determination coefficient to 64% (increased nearly 3.5%) for linear equation and 71% (increased nearly 4.5%) for exponential equation. Regression analysis showed that, Straw yield was positively and significantly affected by morphological characters, except leafiness ( $P = 0.22 > 0.05$ ). However, ANOVA test showed that, straw yield was affected positively by leafiness ( $F = 12.310$ ;  $P < 0.05$ ) Ohlander L, et al. [18].

The non-linear (exponential) equation was better than the linear equation for describing the relationship between straw yield and morphological characters Žáková & Benková [9], because the determination coefficient for exponential (72%) was higher than the determination coefficient for linear (64%; Table 3). Plant height had the greatest influence on straw yield, which explained 60.55% ( $R^2\% = 60.55\%$ ,  $P < 0.05$ ) of the variation for linear equation and explained 66.54% ( $R^2\% = 66.54\%$ ,  $P < 0.05$ ) for exponential equation. These results agree with Capper et al. [19]. The residuals distribution for exponential relationship was better than linear (Figure 3). Studentized residuals indicated that there were thirty-eight points that were more than two standardised residuals away from the expected value for equations (linear and exponential). In conclusion, there was a significant relationship between straw yield and morphological characters. Exponential equation was better than linear equation for studying the relationship between straw yield and morphological characters.



## Conclusion

Multiple regression analysis (linear and non-linear) indicated that there was a significant and positively relationship between yield parameters and morphological characters except leafiness. According to analysis of variance, it can be seen that yield parameters were affected by leafiness, but these relationships were not significant when multiple regression analysis was used.

Non-linear equations (exponential equations) were better than linear equations for studying the relationship between yield parameters and morphological characters, because the determination coefficients in exponential equations were higher than the determination coefficients in linear equations. The residuals distribution for exponential equations were better than the residuals distribution for linear equations. The outlier points in exponential equations was less than the outlier points in linear equations. Consequently, the exponential equations for the study of the relationship between yield parameters and morphological characters are more suitable for forecasting yield than linear equations.

## Acknowledgment

The authors acknowledge the provision of a PhD grant from the University of Damascus, Syria. The author also gratefully acknowledges a Fellowship grant from CARA (the Council for At-Risk Academics).

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DOI: [10.19080/ARTOAJ.2018.14.555907](https://doi.org/10.19080/ARTOAJ.2018.14.555907)

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